

MATHEMATICS SPECIALIST UNIT 1

Section Two: Calculator-assumed

If required by your examination administrator, please
place your student identification label in this box

Student Number: In figures

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In words

Your name

Time allowed for this section

Reading time before commencing work: ten minutes

Working time for this section: one hundred minutes

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer Booklet

Formula Sheet (retained from Section One)

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,
correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper,
and up to three calculators approved for use in the WACE examinations

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this paper

| Section | Number of questions available | Number of questions to be answered | Working time (minutes) | Marks available | Percentage of exam |
|------------------------------------|-------------------------------|------------------------------------|------------------------|-----------------|--------------------|
| Section One: Calculator-free | 7 | 7 | 50 | 52 | 35 |
| Section Two: Calculator-assumed | 13 | 13 | 100 | 98 | 65 |
| Total | | | | 150 | 100 |

Instructions to candidates

- The rules for the conduct of Western Australian external examinations are detailed in the *Year 12 Information Handbook 2015*. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer Booklet.
- You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.
- Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- It is recommended that you **do not use pencil**, except in diagrams.
- The Formula Sheet is **not** to be handed in with your Question/Answer Booklet.

Section Two: Calculator-assumed**(98 Marks)**

This section has **thirteen (13)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time for this section is 100 minutes.

Question 8**(6 marks)**

(a) Determine, giving answers rounded to one decimal place,

(i) the vector projection of $12\mathbf{i} + 37\mathbf{j}$ onto $75\mathbf{i} - 94\mathbf{j}$. (2 marks)

(ii) the vector projection of a force of 60N on bearing 333° onto a force of 30N on a bearing 115° . (2 marks)

(b) Determine the values of a and b given that the vectors $(2, -3)$ and $(a, 6)$ are parallel and the vectors $(2, -3)$ and $(6, b)$ are perpendicular. (2 marks)

Question 9**(8 marks)**

- (a) A teacher has to choose 3 girls and 4 boys to sit in a row for a photograph from a group of 7 girls and 6 boys who volunteered. How many possible ways can she do this, if the boys chosen have to sit next to each other? (4 marks)
- (b) A calculator is programmed to generate random numbers between 0 and 1, such as 0.9155629523 and then round them to one decimal place. How many such numbers must be generated to be certain of obtaining two identical numbers? (2 marks)
- (c) A student has a large selection of music tracks by four different bands (INXS, Spooky Tooth, KISS and The Clash) on their phone. Determine the smallest number of tracks on a playlist so that they will be certain to have at least six tracks by the same band. (2 marks)

Question 10**(7 marks)**

The work done, in joules, by a force \mathbf{F} Newtons in changing the displacement of an object s metres is given by the scalar product of \mathbf{F} and s .

- (a) Calculate the work done by a force $(15, 22)$ N in moving an object $(3, 2)$ m. (1 mark)
- (b) Calculate the work done by a force of 25 N that moves an object 6 m if
- (i) the force acts parallel to the direction of movement. (1 mark)
- (ii) the force acts perpendicular to the direction of movement. (1 mark)
- (iii) the force acts at an angle of 25° to the direction of movement. (1 mark)
- (c) The work done by a force in moving an object $(50, -80)$ cm is 590 joules. If the force acts on a bearing of 115° , determine the magnitude of the force. (3 marks)

Question 11**(8 marks)**

A sub-committee of four, consisting of a chairperson, a secretary and two ordinary members is to be chosen from a larger committee of 20 people (consisting of a chairperson, a secretary and 18 ordinary members).

- (a) Determine, for the sub-committee, the number of possible choices for
- (i) the posts of chairperson and secretary, (1 mark)

 - (ii) the two ordinary members, (1 mark)

 - (iii) the chairperson, secretary and two ordinary members. (2 marks)
- (b) How many sub-committees are possible in which
- (i) the chairman of the larger committee is not included? (2 marks)

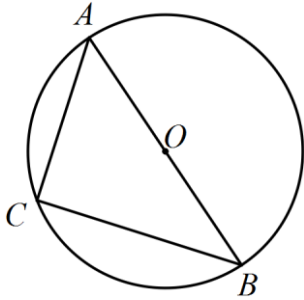
 - (ii) the chairman of the larger committee is chosen as the secretary and the secretary of the larger committee is chosen as an ordinary member? (2 marks)

Question 12

(8 marks)

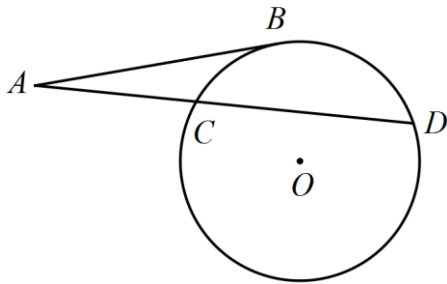
- (a) Determine, with justification, the radius of the circle shown below, given that $AC = 8$ cm and $BC = 15$ cm.

(2 marks)



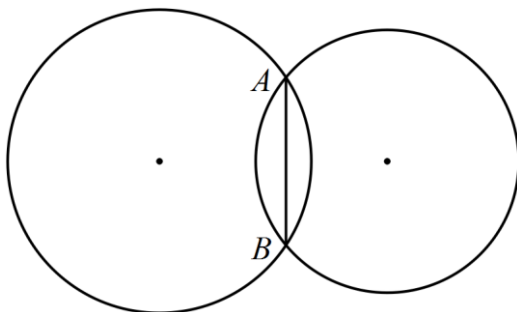
- (b) Determine the length of the chord CD given that the length of the tangent AB is 15 cm and the length of the secant AD is 26 cm.

(3 marks)



- (c) Two circles of radii 18 cm and 24 cm intersect at points A and B . The length of the chord AB is 28 cm. Determine how far apart the centre of the circles lie, giving your answer to three significant figures.

(3 marks)

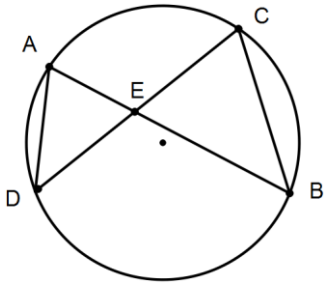


Question 13

(12 marks)

(a) In the diagram below the chords AB and CD intersect at the point E.

The area of $\triangle EAD$ is 15cm^2 .



(i) Explain why $\angle EAD = \angle ECB$ (1 mark)

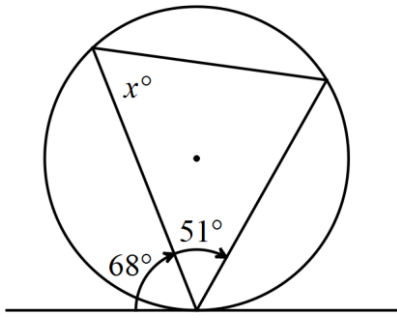
(ii) Prove that $\triangle EAD$ is similar to $\triangle ECB$. (3 marks)

(iii) Use your result from (ii) to show that $AE \times BE = DE \times CE$. (1 mark)

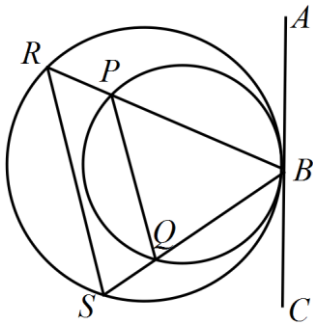
(iv) Find the area of $\triangle ECB$ if $CE = 2 \times AE$. (2 marks)

(b) Determine the size of x in the diagram below.

(2 marks)



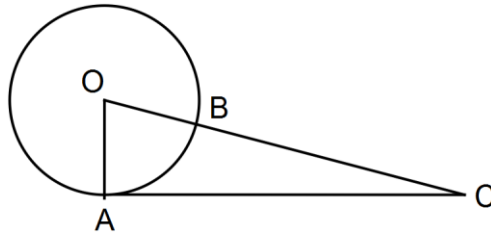
(c) The line segment ABC is a common tangent to both circles shown below. Prove that PQ is parallel to RS . (3 marks)



Question 14

(8 marks)

- (a) In the diagram, AC is a tangent to the circle at A , OC cuts the circle at B and $BC = 2OB$.



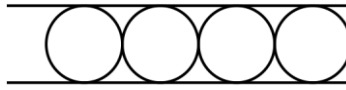
If $\vec{OA} = \mathbf{a}$ and $\vec{OB} = \mathbf{b}$, prove that $\mathbf{a} \cdot \mathbf{b} = \frac{|\mathbf{a}|^2}{3}$.

(4 marks)

- (b) The midpoints of square $ABCD$ are $PQRS$ respectively. Use a vector method to prove that PS is perpendicular to PQ . (4 marks)

Question 15**(7 marks)**

Four different coloured balls (yellow, green, blue, red, purple or orange) are to be placed, one after another, into a tube as shown.



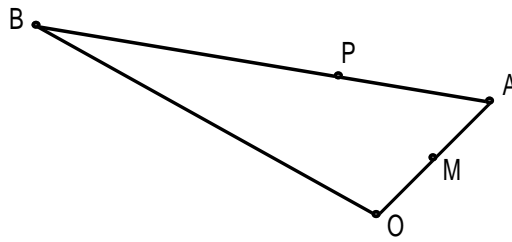
Determine the number of different arrangements of balls that can be made using

- (a) six balls, all of different colours. (1 mark)
- (b) two yellow and two green balls. (1 mark)
- (c) one red, one purple and two blue balls. (1 mark)
- (d) twelve balls, two of each colour. (4 marks)

Question 16

(5 marks)

In the triangle below, $\mathbf{a} = \overrightarrow{OA}$, $\mathbf{b} = \overrightarrow{OB}$, M is the midpoint of OA and P is a point on AB such that $\overrightarrow{AP} : \overrightarrow{PB} = 1 : 3$.



(a) Express each of the following in terms of \mathbf{a} and /or \mathbf{b} .

(i) \overrightarrow{BA} (1 mark)

(ii) \overrightarrow{OP} (1 mark)

(iii) \overrightarrow{MP} (1 mark)

(b) If $\mathbf{a} = \mathbf{i} + 2\mathbf{j}$ and $\mathbf{b} = -9\mathbf{i} + 4\mathbf{j}$, determine $|\overrightarrow{MP}|$. (2 marks)

Question 17**(7 marks)**

A small ball leaves point M and travels with a constant velocity of $2\mathbf{i} + 3\mathbf{j}$ ms⁻¹.

(a) Determine

(i) the distance travelled by the ball in 3 seconds, rounding your answer to two decimal places. (2 marks)

(ii) the time taken for the ball to travel 40 m, to one decimal place. (1 mark)

(b) Determine the least distance between the ball and a point located at $6\mathbf{i} + 5\mathbf{j}$ relative to M. (4 marks)

Question 18

(8 marks)

(a) How many integers between 1000 and 9999 inclusive are multiples of 2, 3 or 7? (4 marks)

(b) Determine the number of different arrangements of three letters selected from those in the word LEVELLED. (4 marks)

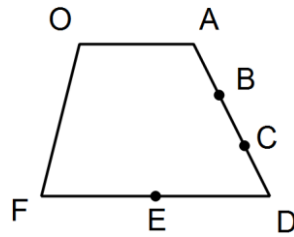
Question 19**(7 marks)**

Location B is 243km away from location A on a bearing of 207° . A helicopter leaves A to fly to B on a day when a steady wind of 35km/h is blowing from the SE. If the helicopter has a cruising airspeed of 185km/h, determine the bearing, to the nearest tenth of a degree, the pilot should steer to fly directly to B and find how long the flight will take, to the nearest minute.

Question 20

(7 marks)

The diagram shows a trapezium in which $\overrightarrow{FD} = 2\overrightarrow{OA}$, E is the midpoint of FD and AD is divided into thirds by points B and C .



Let $\overrightarrow{OA} = \mathbf{m}$ and $\overrightarrow{OF} = \mathbf{n}$.

Use a vector method to prove that $\overrightarrow{FB} = k\overrightarrow{EC}$ and determine the value of k .

Additional working space

Question number: _____

Additional working space

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